

# MATH 53

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① On your homework, you parameterize an ellipse

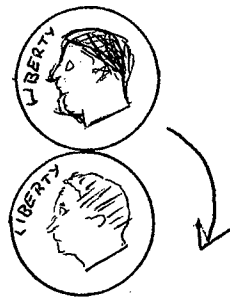
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

[Hint: the circle  $x^2 + y^2 = 1$  satisfies  $x = \cos \theta$ ,  $y = \sin \theta$ .]

What is a parameterization of an ellipse centered at  $(h, k)$ :

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1 ?$$

② Start with two dimes touching, and, holding the bottom fixed, roll the top around the bottom.



(a) How many times does the ~~to~~ moving dime rotate before it returns to its starting location?

(b) What is the path taken by the point on the moving dime that starts out touching the stationary dime?

